

# Response of structure subjected to different Earthquake Ground Motions

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**CERTIFICATE**

This is to certify that this thesis entitled “**RESPONSE OF STRUCTURE SUBJECTED TO DIFFERENT EARTHQUAKE GROUND MOTIONS**” submitted by **Ahmad Milad (111CE0554)** in partial fulfillment for the award of the degree of Bachelor of Technology in Civil Engineering at National Institute of Technology, Rourkela is an authentic work carried out by him under my supervision.

To the best of my knowledge, the matter embodied in this report has not been submitted to any other university/institute for the award of any degree or diploma.

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## **ABSTRACT**

Structural dynamic is a mandatory graduate level course for structural engineering student all around the world. In civil engineering structures are mostly designed based on prescriptive methods of standard codes. Usually loads on these structures are of low magnitude which results in elastic structural behavior. However, strong loads such as a sudden earthquake will lead the structure beyond its elastic limit. Generally 4 kinds of earthquake ground motions are considered such as Fault Normal, Fault Parallel, Near Fault and Far Fault components.

In the current study the performance of a structure in a single degree of freedom system is investigated under different ground motions such as Fault normal and Fault parallel component of the ground motion by dynamic time history analysis method and the analysis is done in the SEISMOSTRUCT software developed by the SEISMOSOFT Company.

The Acceleration, Velocity and displacement curves have been drawn for both Fault Normal and Fault Parallel component of Far Fault and Near Fault ground motion. The values of acceleration, velocity, displacement have been found in every 0.005 seconds, also the values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement has been determined for both components.

The values of PGA, PGV, PGD obtained for fault normal component are higher than the values obtained for the fault parallel component of the ground motion, also the frequencies of fault normal component of ground motion are more than that of the fault parallel component of ground motion.

The values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement of Fault Normal and Fault parallel components don't differ much for Far Fault earthquake ground motions, but they differ much for Near Fault Earthquake ground motions. The response spectrum curves are different for each kind of earthquake ground motions, hence it means that the structure have different responses to each kind of earthquake ground motions.

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## NOTATION AND ABBREVIATIONS

IS	= Indian Standard
THA	= Time History Analysis
RSA	= Response Spectrum Analysis
RC	= Reinforced Concrete
2D	= Two-dimension
3D	= Three-dimension
FN	= Fault Normal
FP	= Fault Parallel
NF	= Near Fault
FF	=Far Fault
$g$	= Acceleration due to gravity ( $m/s^2$ )
EDP	= Engineering Demand Parameters
RHA	= Response History Analysis
SDF	= Single degree of Freedom
PGA	= Peak ground Acceleration
PGV	= Peak ground Velocity
PGD	= Peak ground Displacement
FRP	= Fiber reinforced plastic
HP	= High Pass Filters
LP	= Low Pass Filters
SRS	=Shock Response Spectrum
SRSS	=Square Root of the Sum of the Squares

# **CHAPTER 1**

## **INTRODUCTION**

# **INTRODUCTION:**

## **1.1 General:**

An earthquake is the result of an unexpected release of energy in the Earth's crust that creates seismic waves. The seismicity or seismic action of an area refers to the frequency, type and size of earthquakes practiced over a period of time.

Earthquakes are measured using remarks from seismometers. The moment magnitude is the most common scale on which earthquakes greater than approximately 5 are reported for the entire globe. The more earthquakes smaller than magnitude 5 stated by national seismological observatories are measured mostly on the local magnitude scale, also referred to as the Richter magnitude scale. These two scales are numerically similar over their range of legitimacy. Magnitude 3 or lower earthquakes are mostly almost unnoticeable or weak and magnitude 7 and over potentially causes severe damage over larger areas, dependent on their depth.

The largest earthquakes in historic periods have been of magnitude slightly over 9, although there is no boundary to the possible magnitude. The most recent large earthquake of magnitude 9.0 or larger was a 9.0 magnitude earthquake in Japan in 2011 (as of March 2014), and it was the major Japanese earthquake since records started. Intensity of shaking is measured on the modified scale. The shallower an earthquake (also known as a quake, tremor or temblor) is the result of a sudden release of an earthquake, the more destruction to structures it causes, all else being equal.

At the Earth's surface, earthquakes manifest themselves by trembling and sometimes displacement of the ground. When the epicenter of a large earthquake is situated offshore, the seabed may be displaced adequately to cause a tsunami. Earthquakes can also trigger landslides, and occasionally volcanic movement.

In its most general sense, the word earthquake is used to define any seismic event — whether natural or caused by humans — that produces seismic waves. Earthquakes are caused mostly by rupture of geological faults, but also by other actions such as volcanic activity, landslides, mine blasts, and nuclear tests. An earthquake's point of primary rupture is called its focus or hypocenter. The epicenter is the point at ground level right above the hypocenter.

## **1.2 Seismic waves:**

Seismic waves are waves of energy that travel through the Earth's layers, and are an outcome of an earthquake, explosion, or a volcano that imparts low-frequency acoustic energy. Many other natural and anthropogenic sources create low amplitude waves commonly stated to as ambient vibrations. Seismic waves are studied by geophysicists called seismologists. Seismic wave fields are noted by a seismometer, hydrophone (in water), or accelerometer.

The propagation speed of the waves depends on density and elasticity of the medium. Velocity tends to rise with depth, and ranges from approximately 2 to 8 km/s in the Earth's crust up to 13 km/s in the deep mantle.

Earthquakes generate various types of waves with different velocities; when getting seismic observatories, their different travel time help scientists to trace the source of the earthquake hypocenter. In geophysics the refraction or reflection of seismic waves is used for investigation into the structure of the Earth's interior, and man-made vibrations are regularly generated to investigate shallow, subsurface structures.

## **1.3 Fault:**

A fault is a planar fracture in a volume of rock, across which there has been substantial displacement along the fractures as a consequence of earth movement. Large faults inside the Earth's crust result from the action of plate tectonic forces, with the prime forming the boundaries between the plates, such as subduction zones or renovate faults. Energy release associated with rapid movement on active faults is the origin of most earthquakes.

A fault line is the surface trace of a fault, the line of connection between the fault plane and the Earth's surface.

Since faults do not generally consist of a single, clean fracture, geologists use the term fault zone when referring to the zone of complex deformation allied to the fault plane.

The two sides of a non-vertical fault are known as the hanging wall and footwall. By definition, the hanging wall occurs overhead the fault plane and the footwall occurs beneath the fault. This terminology arises from mining.

Because of friction and the rigidity of the rock, the rocks cannot slide or flow past each other. Rather, stress builds up in rocks and when it reaches a level that go beyond the strain threshold, the accumulated potential energy is dissipated by the relief of strain, which is focused into a plane along which relative motion is accommodated—the fault. Strain is both accumulative and instantaneous depending on the rheology of the rock; the ductile lower crust and mantle stores deformation gradually via shearing, while the brittle upper crust reacts by fracture - instantaneous stress release - to cause motion along the fault. A fault in ductile rocks can moreover release instantaneously when the strain rate is too great. The energy released by instantaneous strain release causes earthquakes, a common phenomenon along transform boundaries.

In the earlier ages structures were only designed for gravity loads and lateral load were not taken in consideration, then when the structure was subjected to lateral loads such as wind load and earthquake loads then it was getting damaged, so the engineers decided to make wind resistant and earthquake resistant structures.

In here we will be talking about earthquake resistant structures, and for doing such we need the ground acceleration data for the site where the structure is located and then we will prepare the design according to the ground acceleration history data.

In this research we will be taking 4 kinds of earthquakes mentioned below:

1. Far Fault Earthquake

- 1a. Fault Parallel component

- 1b. Fault Normal component

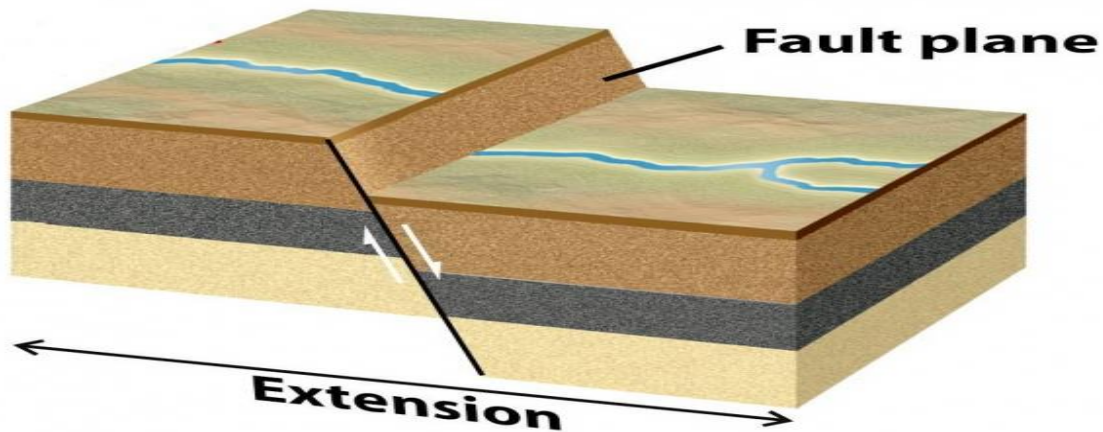
2. Near Fault Earthquake

- 2a. Fault Parallel component

- 2b. Fault Normal component

### 1.3.1 Fault Parallel Earthquake:

The component of ground motion parallel to the fault plane is called fault parallel. Fig.1.1 shows fault plane.

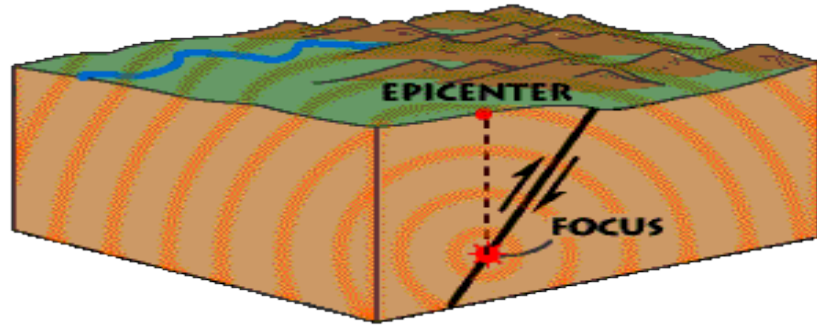


**Fig.1.1: Fault plane**

### 1.3.2 Fault Normal Earthquake:

The component of ground motion normal to fault plane is called fault normal earthquake. However the fault normal component is of higher peak ground acceleration (PGA) than the fault parallel component at the same recording station. Fig.2.2 shows the epicenter and focus of the earthquake.





**Fig.1.2: Epicenter and Focus of the earthquake**

### **1.3.3 Near Fault Earthquake:**

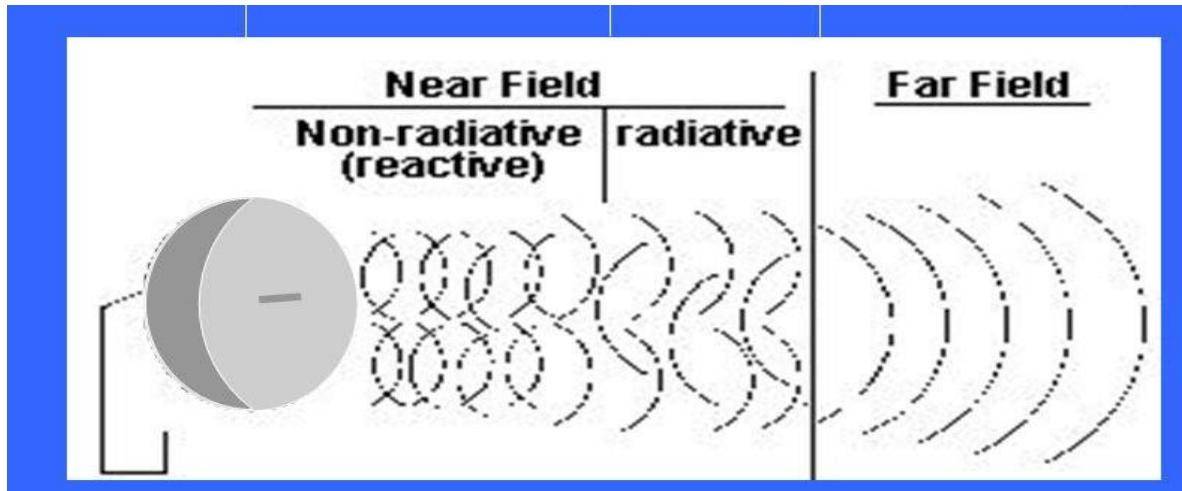
When the site of the structure is near to the epicenter of the earthquake then it is called Near Field Earthquake.

### **1.3.4 Far Fault Earthquake:**

When the site where the structure is located is far from the epicenter of the earthquake then it is called Far Field Earthquake; however there is no definite distance over which a site may be classified as in near or far-field

.It is recognized that the characteristics of near-field earthquake ground motions are different from those records in the far-field. Fig.1.3 shows the near field and far field earthquake.

The values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement of Fault Normal and Fault parallel components don't differ much for Far Fault earthquake ground motions, but they differ much for Near Fault Earthquake ground motions.



**Fig1.3: Near Field and Far Field Earthquake Ground Motion**

#### **1.4 Objective and Scope:**

To study the differences in structural responses against different earthquake ground motions and we compare the results as follows:

1. Far-field/Near-field
2. Fault-parallel/Fault-normal

To perform dynamic time history analysis on a structure in single degree of freedom system with the use SEISMOSTRUCT software.

To compare the associated Response Spectrums for Fault Normal and Fault Parallel components of both kinds of earthquake ground motions.

## **1.5 Methodology:**

1. Studied Literature review for understanding the characteristics of different earthquake ground motions.
2. Collected different earthquake ground motions from strong motion database.
3. Learned dynamic analysis of structures.
4. Learned response spectrum analysis.
5. Learned SEISMOSTRUCT software.
6. Modeled the structure (single degree of freedom system) in SEISMOSTRUCT software and analyzed it for fault normal and fault parallel component of ground motion.
7. Compared the results (acceleration, displacement or velocity) for fault normal and fault parallel component of far fault and near fault ground motion.
8. Compared the associated Response Spectrums.

# **CHAPTER 2**

# **LITERATURE REVIEW**

## **LITERATURE REVIEW:**

### **2.1 General**

**Durgesh C. Rai (2005)** has developed guidelines for seismic evaluation and firming up of buildings. The document was established as part of project “Review of Building Codes and Preparation of Commentary and Handbooks” presented to Indian Institute of Technology Kanpur by the Gujarat State Disaster Management Authority (GSDMA), Gandhinagar through World Bank finances. This document is predominantly concerned with the seismic evaluation and strengthening of current buildings and it is proposed to be used as a guide.

**Douglas Dreger, Gabriel Hurtado, Anil K. Chopra, Shawn Larsen, 2007** studied Near fault seismic ground motion and got that For a vertical strike-slip fault the FN ground motions are the same on each side of the fault, whereas the FP component doesn't have equal amplitude but contrary static offset. The corresponding velocity pulses are the equal on each side of the fault for the FN component, but opposite in sign on the FP component. This degree of symmetry vanishes when the fault is dipping due to the uncontrolled free-surface. Motions on the hanging block side are greater due to the free-surface effect, and because a larger fraction of the fault surface is nearer to the stations on the side of the fault that dips under the recording stations.

**Kim and Elnashai (2009)** observed that buildings for which seismic design was performed using contemporary codes persisted the earthquake loads. However the vertical motion significantly reduced the shear capacity in vertical members.

**Abu Lego (2010)** Site Response Spectra was used to study the response of buildings because of earthquake loading. . According to the Indian standard for Earthquake resistant design (IS: 1893), the seismic force or base shear rest on on the zone factor (Z) and the average response acceleration coefficient ( $S_a/g$ ) of the soil kinds at thirty meter depth with suitable adjustment depending upon the depth of foundation. In the present study an effort has been made to generate response spectra using site definite soil parameters for some sites in Arunachal Pradesh and Meghalay in seismic zone V and the generated response spectra is used to analyze some structures using the design software STAAD Pro.

**Mr. S. Yaghmaei-Sabegh and MR. N. Jalali-Milani, 2012** studied Pounding force response spectrum for near-field and far-field earthquakes and got the result that insufficient separation distance between neighboring buildings with out-of-phase response would rise the probability of pounding during an earthquake and may cause serious damages to the structures. A rational estimation of the maximum impact force would support us to control the extent of damages in different structures. The pounding force response spectrum, which shows the value of maximum impact force as a function of the structural vibration stages, is considered in this paper. It is well-known that solid ground motion in the near-field area has different characteristics from far-field ones. In this paper, pounding force response spectra for elastic structures subjected to near-field and far-field ground motions are shown. Both of the neighboring buildings were modeled simply as Single Degree Of Freedom (SDF) systems and pounding effect has been replicated by applying the nonlinear viscoelastic model. In the analysis, the effect of altered parameters, such as mass, damping ratio has been studied. The effects of gap distance on maximum pounding force due to near- and far-field earthquake ground motions were studied comprehensively. As a result, the characteristics of earthquake ground motions alongside with the properties of structures should be considered in gap distance controlling amongst adjacent buildings.

**Mr. J.C. Reyes and Mr. E. Kalkan, 2012** studied Relevance of Fault-Normal/Parallel and Maximum Direction Rotated Ground Motions on Nonlinear Behavior of Multi-Story Buildings and got that The existing state-of-practice in U.S. is to rotate the as-recorded couple of ground motions to the fault normal and fault-parallel (FN/FP) directions before they are used as input for three-dimensional nonlinear response history analyses (RHAs) of structures. It is presumed that this approach will lead to two sets of responses that cover the range of possible responses over all non-redundant rotation angles. Thus, it is considered to be a conservative method appropriate for design verification of new structures. Based on the 9-story symmetric and asymmetric buildings, the effect that the angle of rotation of the ground motion has on several engineering demand parameters (EDPs) has been observed in nonlinear-inelastic domain.

**Mr. Kalkan, and Mr. Kwong, 2012** studied Evaluation of fault-normal/fault-parallel directions rotated ground motions for response history analysis of an instrumented six-story building and got that depending on regulatory building codes in United States (for example, 2010 California Building Code), at least two horizontal ground-motion components are required for three-dimensional (3D) response history analysis (RHA) of structures. For sites within 5 km of an active fault, these records should be divided to fault-normal/fault-parallel (FN/FP) directions, and two RHA analyses should be performed individually (when FN and then FP are aligned with the sloping direction of the structural axes). It is assumed that this tactic will lead to two sets of responses that envelope the range of probable responses overall no redundant rotation angles.

This assumption is studied here using a 3D computer model of a six-story reinforced-concrete instrumented building subjected to an ensemble of bidirectional near-fault ground motions. Peak responses of engineering demand parameters (EDPs) were obtained for rotation angles ranging from  $0^\circ$  through  $180^\circ$  for calculating the FN/FP directions. It is verified that rotating ground motions to FN/FP directions (1) does not always lead to the maximum responses over all angles, (2) does not always envelope the range of possible responses, and (3) does not provide maximum responses for all EDPs instantaneously even if it provides a maximum response for a specific EDP.

**Yen-Po Wang (2014)** introduced the basics of seismic base isolation as an effective technique for seismic design of structures. Spring-like isolation bearings concentrated earthquake forces by changing the fundamental time period of the structure so as to avoid resonance. Sliding-type isolation bearings filter out the earthquake forces via discontinuous sliding interfaces and forces were prohibited from getting transmitted to the superstructure due to the friction. The design of the base isolation system involved finding out the base shear, bearing displacement etc. in accordance with site-specific conditions.

### 3.2 Summary of literature Review:

1. The fault-normal component of numerous, but not all, near-fault ground motions carry out much bigger deformation and strength demands compared to the fault-parallel component over a wide range of vibration periods. In contrast, the two components of most far-fault records are quite similar in their demands.
2. The strength and deformation demands of the fault-normal component of many near fault ground motions are larger than that of the fault-parallel component primarily because the peak acceleration, velocity and displacement of the previous are much larger, although its response amplification factors are lesser.
3. The velocity-sensitive spectral region for the fault-normal component of near-fault records is much thinner, and their acceleration-sensitive and displacement-sensitive regions are much broader, compared to far-fault motions. The narrower velocity-sensitive region of near-fault records is shifted to lengthier periods.
4. For the same ductility factor, near-fault ground motions impose a higher strength demand in their acceleration-sensitive region compared to far-fault motions, with both demands stated as a fraction of their respective elastic demands. This systematic difference is primarily because of the difference between the  $T_c$  values for the two sorts of excitations. If the period scale is normalized relative to the  $T_c$  value, the strength reduction factors for the two types of motions are similar over all spectral regions.



# **CHAPTER 3**

# **HISTORY OF**

# **STRUCTURAL**

# **ANALYSIS**

### **3.1 History of Structural Analysis**

A structure refers to a system of two or more connected parts used to resist a load. It may be considered as a gathering of two or more basic components linked to each other so that they carry the design loads securely without causing any serviceability failure. Once initial design of a structure is fixed, the structure then must be analyzed to make sure that it has its essential strength and rigidity. The loadings are supposed to be taken from particular design codes and local specifications, if any. The forces in the members and the displacements of the joints are found using the theory of structural analysis. The entire structural system and its loading conditions might be of complex nature, so to make the analysis easier, certain simplifying assumptions associated to the material quality, member geometry, nature of applied loads, their distribution, the type of connections at the joints and the support conditions are used. This shall assist making the process of structural analysis simpler to quite an extent.

### **3.2 Methods of structural analysis**

When the number of unknown reactions or the number of internal forces surpasses the number of equilibrium equations existing for the purpose of analysis, the structure is called a statically indeterminate structure. Many structures are statically indeterminate. This indeterminacy may be as a result of additional supports or extra members, or by the general form of the structure. While analyzing any indeterminate structure, it is important to satisfy equilibrium, compatibility, and force-displacement conditions for the structure. The fundamental methods to analyze the statically indeterminate structures are discussed below.

#### **3.2.1 Force method**

The force method developed first by James Clerk Maxwell and further developed later by Otto Mohr and Heinrich Muller-Breslau was one of the first methods available for analysis of statically indeterminate structures. This method is also known as compatibility method or the method of consistent displacements. In this method, the compatibility and force displacement requirements for the particular structure are first defined in order to determine the redundant forces. Once these forces are determined, the remaining reactive forces on the given structure are found out by satisfying the equilibrium requirements.

### **3.2.2 Displacement method**

In the displacement method, first of all load-displacement relations for the members of the structure are determined and then the equilibrium requirements for the same are satisfied. The unknowns in the equations are displacements. Unknown displacements are written in terms of the loads or forces by using the load-displacement relations and then these equations are solved to find out the displacements. As the displacements are found out, the loads are determined from the compatibility and load- displacement equations. Some classical techniques used to apply the displacement method are discussed.

### **3.2.3 Slope deflection method**

This method was first invented by Heinrich Manderla and Otto Mohr to study the secondary stresses in trusses and was after developed by G. A. Maney in order to extend its application to analyze indeterminate beams and framed structures. The basic assumption of this technique is to consider the deformations caused only by bending moments. It is supposed that the effects of shear force or axial force deformations are negligible in indeterminate beams or frames. The fundamental slope-deflection equation states the moment at the end of a member as the superposition of the end moments caused due to the external loads on the member, with the ends being assumed as restrained, and the end moments caused by the displacements and actual end rotations. Slope-deflection equations are applied to every member of the structure. Using proper equations of equilibrium for the joints along with the slope-deflection equations of each member, a set of simultaneous equations with unknowns as the displacements are obtained. Once the values of these displacements are determined, the end moments are found using the slope-deflection equations.

### **3.2.4 Moment distribution method**

This method of analyzing beams and multi-storey frames using moment distribution was presented by Prof. Hardy Cross in 1930, and is also sometimes known as Hardy Cross method. It is an iterative method. Initially all the joints are temporarily restrained against rotation and fixed end moments for each of the member are written down. Every joint is then released one by one in succession and the unbalanced moment is distributed to the ends of the members in the ratio of their distribution factors. These distributed moments are then carried over to the far ends of the joints. Again the joint is temporarily restrained before going to the next joint. Same set of operations are done at each joint till all the joints are completed and the results achieved are up to desired accuracy. The method does not involve solving a number of simultaneous equations, which may get pretty complicated while dealing with large structures, and is thus preferred over the slope-deflection method.

### **3.2.5 Kani's method**

This method was first established by Prof. Gasper Kani of Germany in the year 1947. This is an indirect extension of slope deflection method. This is an effective method due to simplicity of moment distribution. The method offers an iterative scheme for applying slope deflection method of structural analysis. Whereas the moment distribution method reduces the number of linear simultaneous equations and such equations needed are equal to the number of translator displacements, the number of equations needed is zero in case of the Kani's method.

# **CHAPTER 4**

# **SEISMIC ANALYSIS**

## 4.1 Time History Analysis:

Dynamic analysis defines time-dependent displacements and forces due to dynamic loads or nodal accelerations. It can be executed on linear or nonlinear models, and Linear or nonlinear equilibrium equations are solved by the Newmark-beta method. Acceleration functions can also be used for seismic analysis. In this case it is suggested to obtain proper seismic accelerograms and assign these functions to support nodes to examine the effects of the earthquake. Its disadvantage is that it cannot be joined with other load types automatically.

In time history analysis there are a number of ways to numerically integrate the fundamental equation of motion. Many of these are discussed in text books including the referenced texts included in this document. Visual Analysis uses the Newmark method of numerical integration which is known as a generalization of the linear acceleration method.

To perform a time history analysis, you must first generate a new time history case. This is done on the Load menu in Visual Analysis. The dialog will need a name for the time history case and the parameters discussed above must be entered. The second page of the dialog is where you state the type of loading you would like applied to the structure.

When in a Result View, the time history case is selected in the status bar like any other load case in Visual Analysis. The exceptional characteristic of time history cases is you can see results for every time step. A very beneficial way to look at results is to use the graph feature.

There are three main report items existing for time history load cases: Time History Cases, Forcing Function Details, and Forcing Function Summary. The Time History Cases item consists of a number of items with the most common ones being the number of time steps, time step increment, and the forcing type. The Forcing Function Details and Forcing Function Summary report items are very similar. They both include the time history case name, the forcing type, the location of the source text file that was used (if applicable) and the number of data points.

The only additional information the Forcing Function Details report gives is the data that was read in from the text file. Note that many of the static reports are presented at a specific time increment in a time history analysis. For example, you can see member internal forces at any of the time increments during the analysis. Also, the use of enveloped results becomes very convenient for processing time history results. Logically, using an envelope would rapidly allow you to view the overall maximum and minimum extremes for the time history case or for multiple load cases.

## **4.2 Response Spectrum Analysis:**

Response-spectrum analysis is a linear-dynamic statistical analysis method which determines the contribution from each natural mode of vibration to specify the likely maximum seismic response of an essentially elastic structure. Response-spectrum analysis provides vision into dynamic behavior by measuring pseudo-spectral acceleration, velocity, or displacement as a function of structural period for an available time history and level of damping. It is practical to envelope response spectra such that a smooth curve signifies the peak response for each realization of structural period.

Response-spectrum analysis is suitable for design decision-making as it relates structural type-selection to dynamic performance. Structures of smaller period experience larger acceleration, whereas those of lengthier period experience larger displacement. Structural performance objectives should be taken into account during initial design and response-spectrum analysis.

A response spectrum is a plot of the peak or steady-state response (displacement, velocity or acceleration) of a series of oscillators of different natural frequency that are forced into motion by the equivalent base vibration or shock. The resulting plot can then be used to pick off the response of any linear system, given its natural frequency of oscillation. One such use is in evaluating the peak response of buildings to earthquakes. The science of strong ground motion may use some values from the ground response spectrum (calculated from recordings of surface ground motion from seismographs) for correlation with seismic damage.

If the input used in calculating a response spectrum is steady-state periodic, then the steady-state result is noted. Damping must be existing, or else the response will be infinite. For transient input (such as seismic ground motion), the peak response is testified. Some level of damping is generally assumed, but a value will be found even with no damping.

Response spectra can also be used in calculating the response of linear systems with several modes of oscillation (multi-degree of freedom systems), although they are only precise for low levels of damping. Modal analysis is executed to identify the modes, and the response in that mode can be chosen from the response spectrum. These peak responses are then joined to estimate a total response. A classic combination method is the square root of the sum of the squares (SRSS) if the modal frequencies are not close. The result is different from that which would be calculated directly from an input, since phase information is lost in the process of creating the response spectrum.

The main restriction of response spectra is that they are only generally applicable for linear systems. Response spectra can be produced for non-linear systems, but are only applicable to systems with the same non-linearity, although efforts have been made to develop non-linear seismic design spectra with extensive structural application. The results of this cannot be directly united for multi-mode response.

### **4.3 Difference between THA and RSA:**

Time history analysis provides more precise results than the response spectrum analysis and can be used even if nonlinear elements are defined in the model.

In time history analysis the structural response is calculated at a number of subsequent time instants. In other words, time histories of the structural response to an assumed input are obtained and a result. In response spectrum analysis the time progress of response cannot be computed. Only the maximum response is predicted. No data is available also about the time when the maximum response occurs.



It is worthwhile to know that a time history, convolved with the transfer function of a single degree of freedom (SDF) system is what creates the response spectrum. More in detail, the frequency axis of the response spectrum is not normal frequency but rather the natural frequency of the SDF system.

The procedure simplifies downstream valuation of maximum response and allows combination of numerous time histories. In essence, what is required is simple modal analysis, the multiplication of the modal response by the response spectrum amplitude at the natural frequency of the calculated modes.

Also, there is a change between shock response spectrum (SRS) and response spectrum analysis where the former refers to (absolute) fixed frame motion of the SDF mass and the latter refers to SDF base-mass relative motion.

The procedure is used for shocks, seismic analysis, packaging design and several other analysis where simple answers are hard found.

Response spectrum considers the spectrum of a response quantity like acceleration with respect to frequency. This spectrum is used to produce acceleration coefficients for different masses which in turn provide the force.

On the other hand, time history analysis uses the time history of input force or acceleration directly which is then united to get the response.

#### **4.4 About the Software:**

SeismoStruct is Finite Element package capable of calculating the large displacement behavior of space frames under static or dynamic loading, taking care of both geometric nonlinearities and material inelasticity. Concrete, steel and FRP material models are existing, together with a huge library of 3D elements that can be used with a wide variety of pre-defined steel, concrete and composite section configurations. The program has been widely quality-checked and validated, as described in its Verification Report. Some of the more vital features of SeismoStruct are shown in what follows:

- Completely visual interface. No input or configuration files, programming scripts or any other time-taking and complex text editing necessities.
- Full combination with the Windows environment. Input data created in worksheet programs, such as Microsoft Excel, may be pasted to the SeismoStruct input tables, for stress-free pre-processing. Conversely, all information available within the graphical interface of SeismoStruct can be copied to software applications (e.g. to word processing programs, such as Microsoft Word), including input and output data, high quality graphs, the models' deformed and undeformed shapes and much more are available.
- With the Wizard facility the user can generate regular/irregular 2D or 3D models and run all types of analysis on the fly. The whole procedure takes no more than a few seconds.
- Seven different kinds of analysis: dynamic and static time-history, conventional and adaptive pushover, incremental dynamic analysis, eigenvalue, and non-variable static loading.
- The applied loading consist of constant or variable forces, displacements and accelerations at the nodes. The variable loads can vary proportionally or independently in the time domain.
- The program can help in both material inelasticity and geometric nonlinearity.
- A large number of different reinforced concrete, steel and composite sections are available.
- The spread of inelasticity along the member length and across the section depth is clearly modelled in SeismoStruct allowing for precise estimation of damage accumulation.
- Numerical stability and exactness at very high strain levels enabling accurate determination of the collapse load of structures.
- The innovative adaptive pushover procedure. In this pushover method the lateral load distribution is not kept constant but is continuously updated, according to the modal shapes and participation factors determined by eigenvalue analysis carried out at the current step. In this way, the stiffness state and the period elongation of the structure at every step, as well as higher mode effects, are accounted for. In particular the displacement-based variant of the approach, due to its ability to update the lateral displacement patterns according to the constantly changing modal properties of the system.

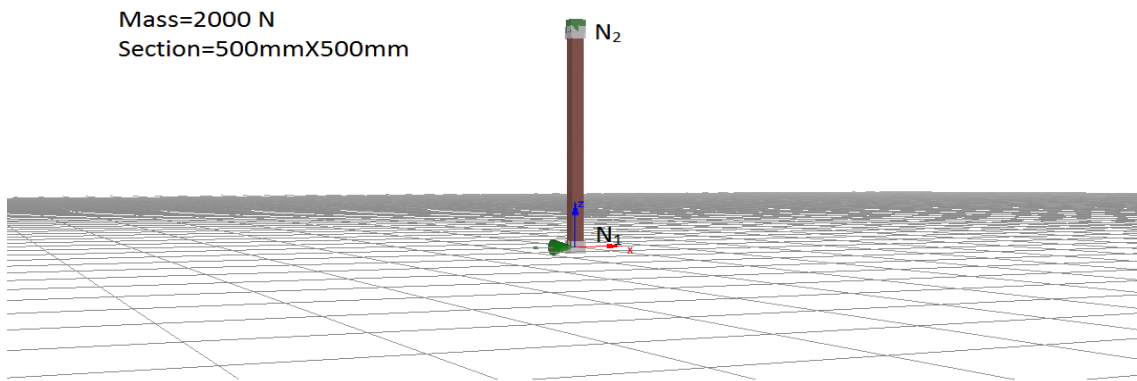
- SeismoStruct has the ability to rapidly subdivide the loading increment, each and every time convergence problems arise. The level of subdivision depends on the convergence difficulties came across. When convergence difficulties are overwhelmed, the program automatically rises the loading increment back to its original value.
- SeismoStruct's processor features real-time plotting of displacement curves and deformed shape of the structure, with the ability of pausing and re-starting the analysis.
- Performance criteria can also be set, permitting the user to find the instants at which different performance limit states (e.g. non-structural damage, structural damage, and collapse) are reached. The sequence of cracking, yielding, failure of members throughout the structure can also be readily obtained.
- Advanced post-processing facilities, including the ability to custom-format all derived plots and deformed shapes, thus growing productivity of users.

# **CHAPTER 5**

## **RESULTS**

## 5.1 Design:

First of all a simple structure was designed in single degree of freedom system with length equal to 10m and mass equal to 2000 N from an elastic material. It's having a square cross section of 0.5m\*0.5m.



**Fig 5.1: Single Degree of Freedom Model designed in SEISMOSTRUCT**

## 5.2 Far Fault Earthquake:

### 5.2.1 Input Data

After that the ground motion data was downloaded from PEER strong motion database.

The analysis are performed for 2 sets of ground motion records (FN and FP) for the “Oroville 1975/08/08 07:00” earthquake at 1543 DWR Garage station. The acceleration time history was recorded for every 0.005 seconds.

PEER Strong Motion Database: Search - Microsoft Internet Explorer

Address: <http://peer.berkeley.edu/smcat/search.html>

**PEER Strong Motion Database**

Introduction Browse **Search** Documentation Providers Credits

**1: Search earthquake or station characteristics and peak values**

Earthquake: Coalinga 1983/05/02 23:42

Mechanism: Any

Magnitude (Range): -  -  ☐ ML ☐ M ☐ MS ☒ Any

Distance (km): -  -  ☐ Closest ☐ Hypocentral ☐ Projection of fault plane (JB distance) ☒ Any

Site Classification: USGS  Any (Compare to NEHRP classifications)

Geomatrix: Any

Taiwan CWB: Any

Mapped Local Geology: Any

Instrument Housing: Any

Data Source: Any

PGA (g): -  -  Range 0.001 ... 2.086

PGV (cm/sec): -  -  Range 0.1 ... 263.1

PGD (cm): -  -  Range 0.01 ... 430.00

Search Clear

Fig 5.2: PEER Strong Motion Database

## P0117: Earthquake and Station Details

Oroville 1975/08/08 07:00 Magnitude: M ( 4.7 ) Ml ( 4.9 ) Ms ( )	Station: 1543 DWR Garage Data Source: <a href="#">CIT</a>
Distance (km): Closest to fault rupture ( ) Hypocentral ( 6.5 ) Closest to surface projection of rupture ( )	Site conditions: Geomatrix or CWB ( A ) USGS ( )

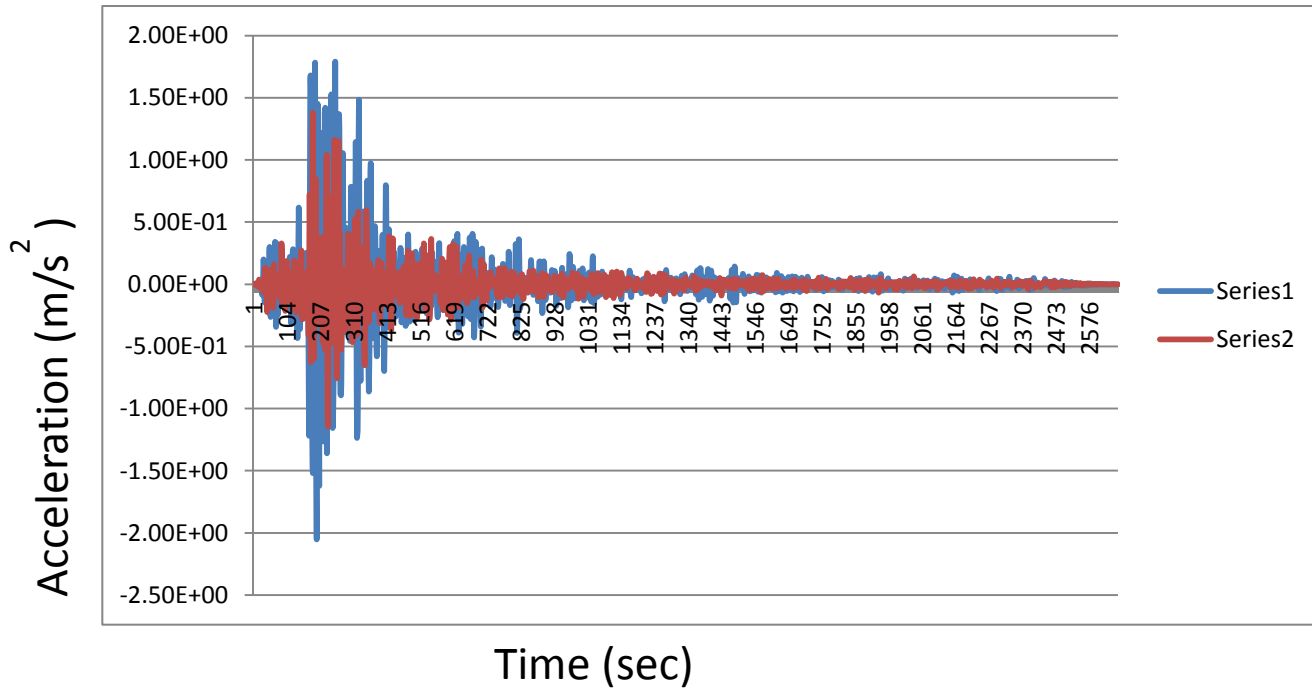
### Downloaded Input data

Record/Component	HP (Hz)	LP (Hz)	PGA (g)	PGV (cm/s)	PGD (cm)	Acceleration	Velocity	Displacement	Spectra
OROVILLE/ D-DWRDWN	5.0	40.0	0.106	0.7	0.01	<a href="#">ATH</a>	<a href="#">VTH</a>	<a href="#">DTH</a>	<a href="#">0.5%</a> <a href="#">1%</a> <a href="#">2%</a> <a href="#">3%</a> <a href="#">5%</a> <a href="#">7%</a> <a href="#">10%</a> <a href="#">15%</a> <a href="#">20%</a>
OROVILLE/ D-DWR090	1.5	50.0	0.141	1.1	0.04	<a href="#">ATH</a>	<a href="#">VTH</a>	<a href="#">DTH</a>	<a href="#">0.5%</a> <a href="#">1%</a> <a href="#">2%</a> <a href="#">3%</a> <a href="#">5%</a> <a href="#">7%</a> <a href="#">10%</a> <a href="#">15%</a> <a href="#">20%</a>
OROVILLE/ D-DWR180	3.0	40.0	0.209	1.8	0.02	<a href="#">ATH</a>	<a href="#">VTH</a>	<a href="#">DTH</a>	<a href="#">0.5%</a> <a href="#">1%</a> <a href="#">2%</a> <a href="#">3%</a> <a href="#">5%</a> <a href="#">7%</a> <a href="#">10%</a> <a href="#">15%</a> <a href="#">20%</a>

HP = High Pass and LP = Low Pass Filters

Spectra are available for 0.5 - 20% damping.

Source record processed by Pacific Engineering.



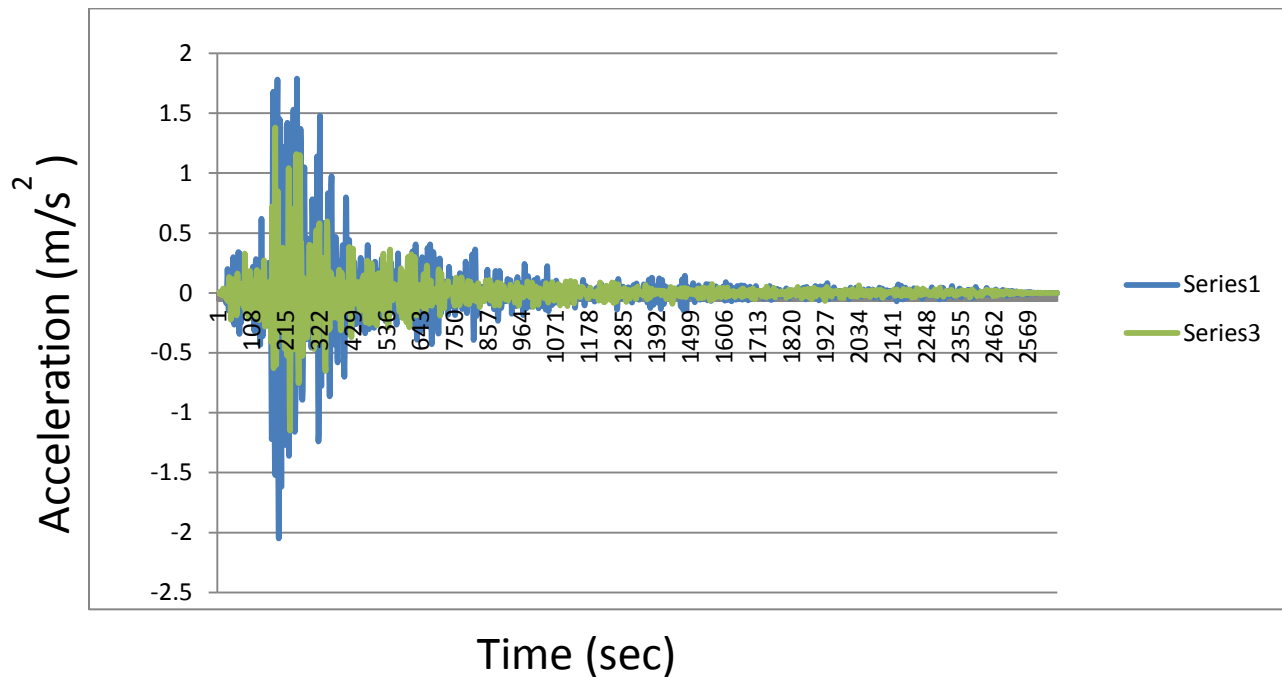
**Graph 5.1: Acceleration curve (Fault Normal & fault parallel Input data)**

## 5.2.2 Output data:

### 5.2.2.1 Time History Analysis:

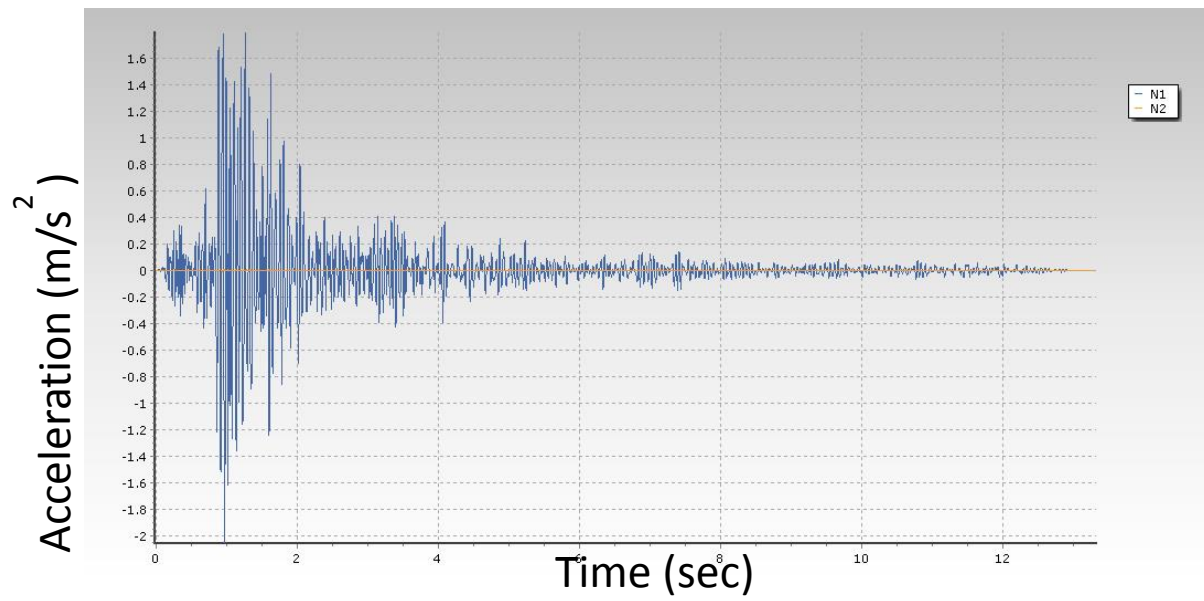
The effect of the downloaded input ground motion data has been investigated on the structure (SDF system) using the dynamic time history analysis.

After performing the dynamic time history analysis we have got the output data for both fault normal and fault parallel components of Far Fault ground motions , and also the curves for (acceleration, velocity and displacement) versus time were obtained which are shown in the following figures:

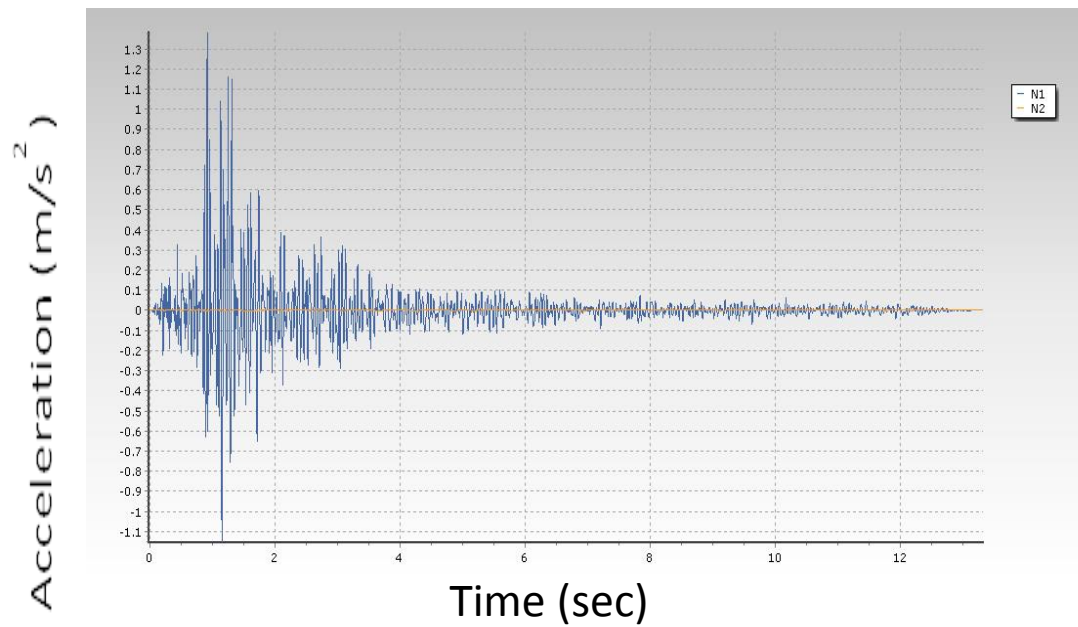


**Graph 5.2: Acceleration curve (Fault Normal & fault parallel)**

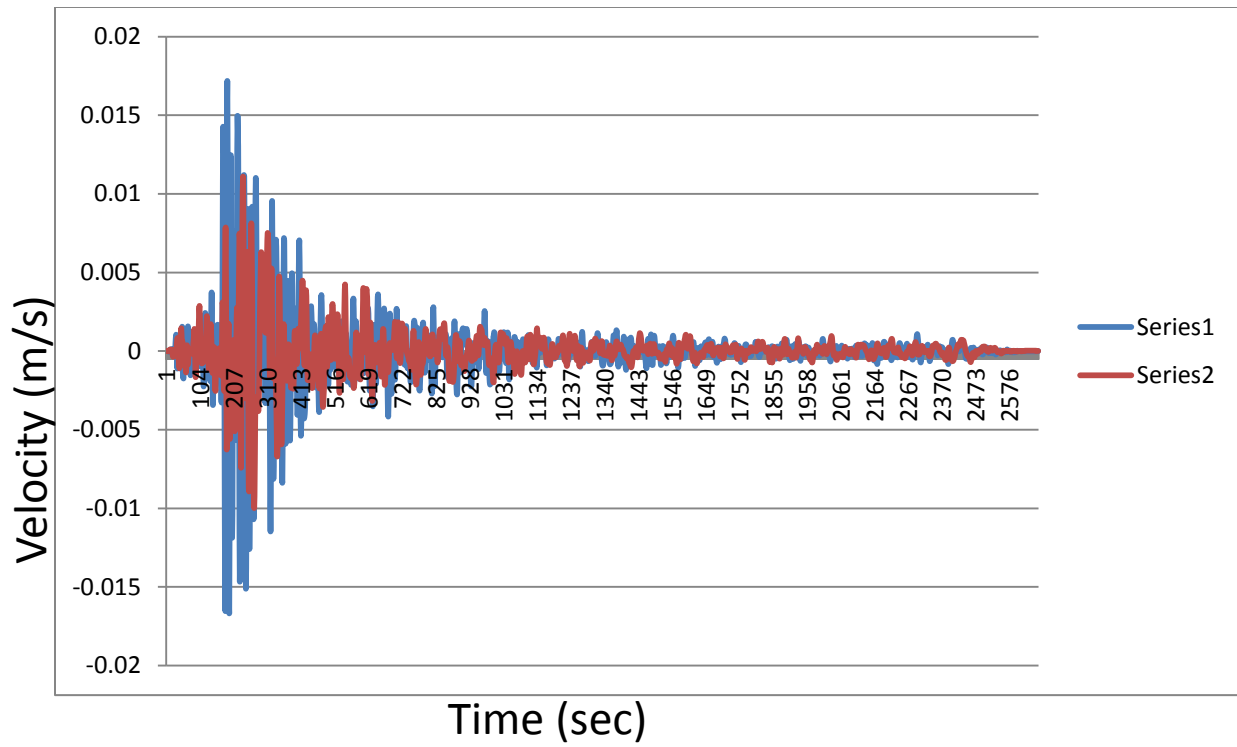




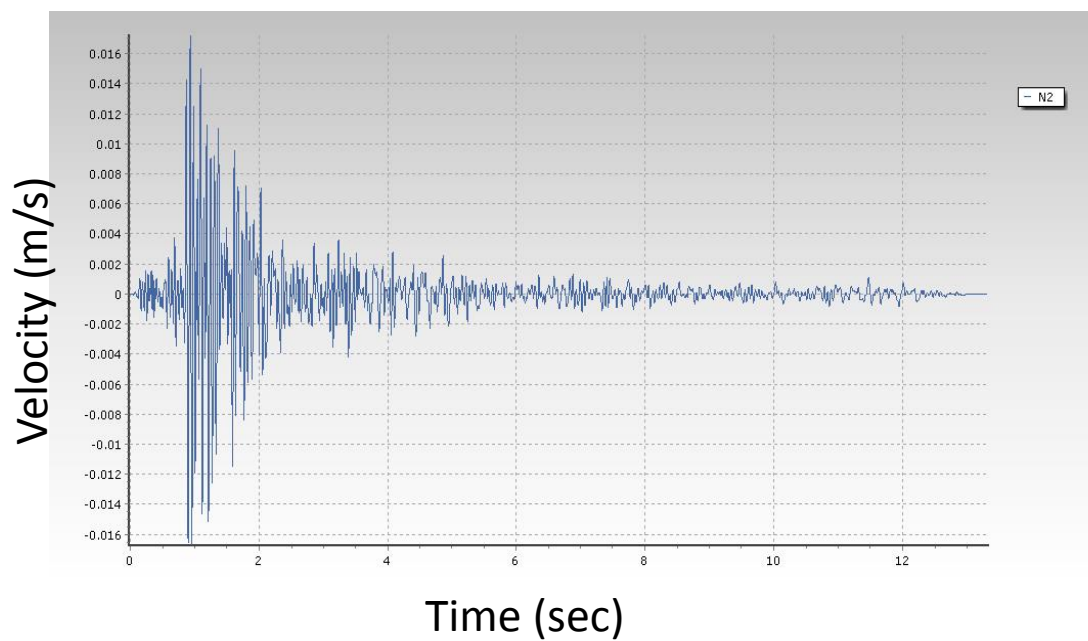
**Graph 5.3: Acceleration curve (Fault Normal)**



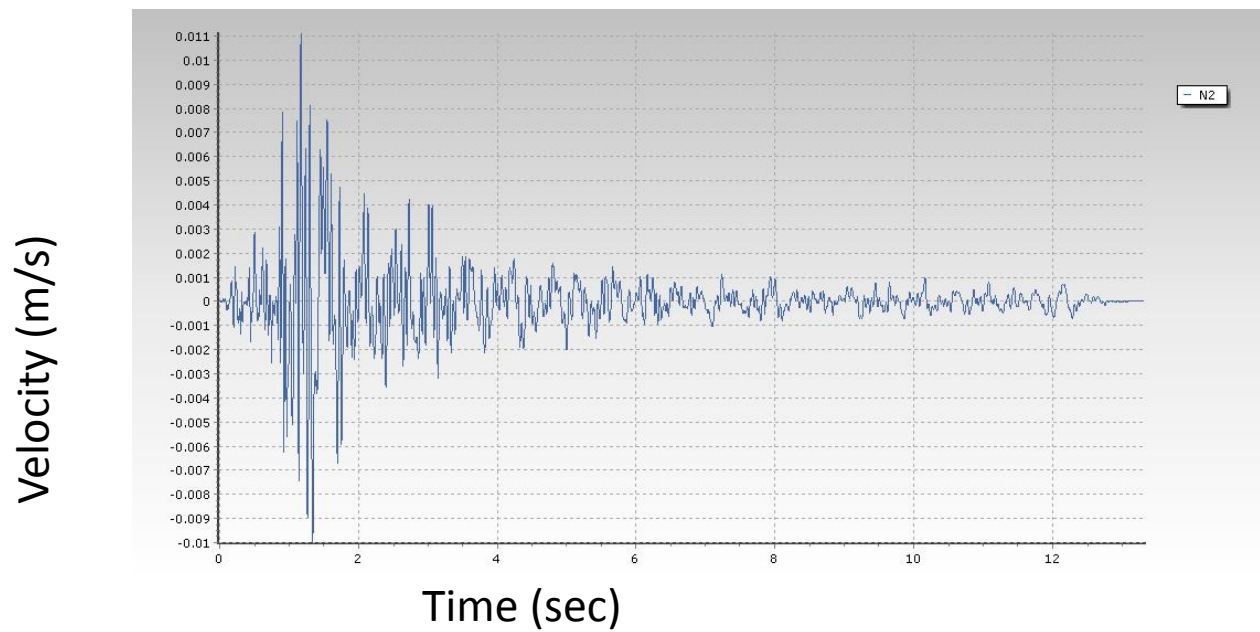
**Graph 5.4: Acceleration curve (Fault Parallel)**



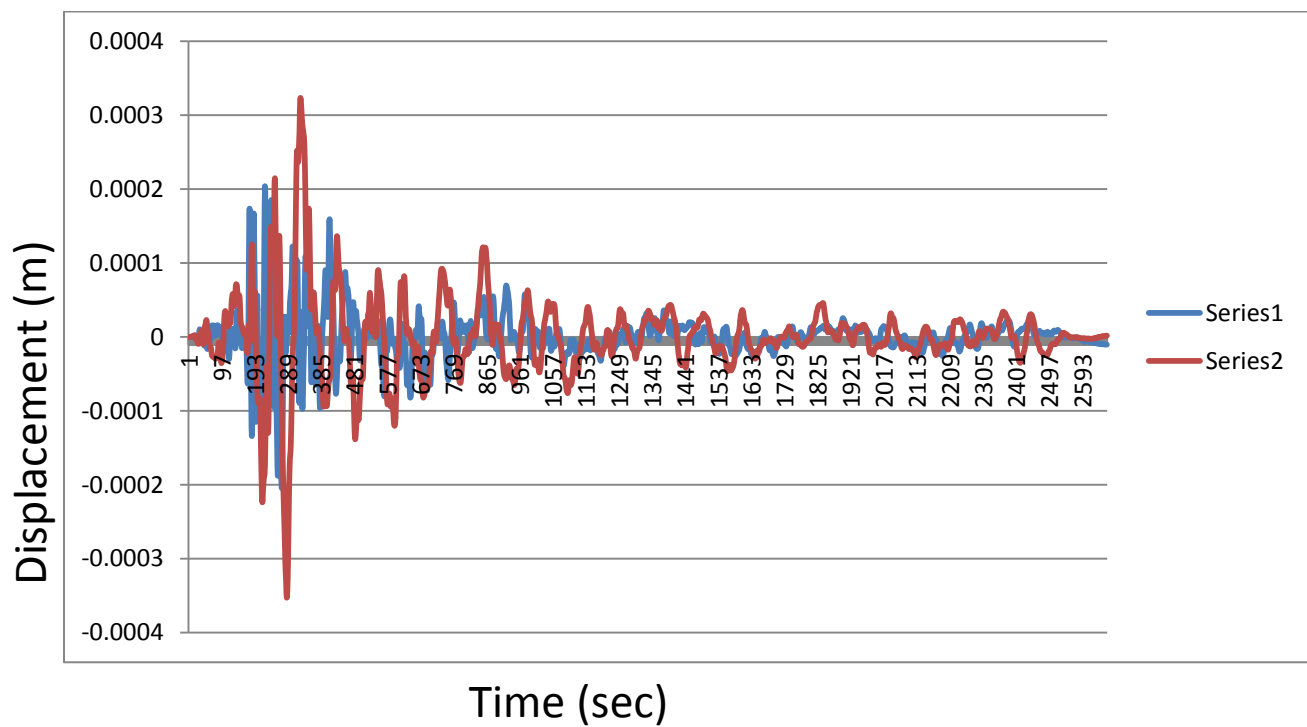
**Graph 5.5: Velocity Curve (Fault Normal & Fault Parallel)**



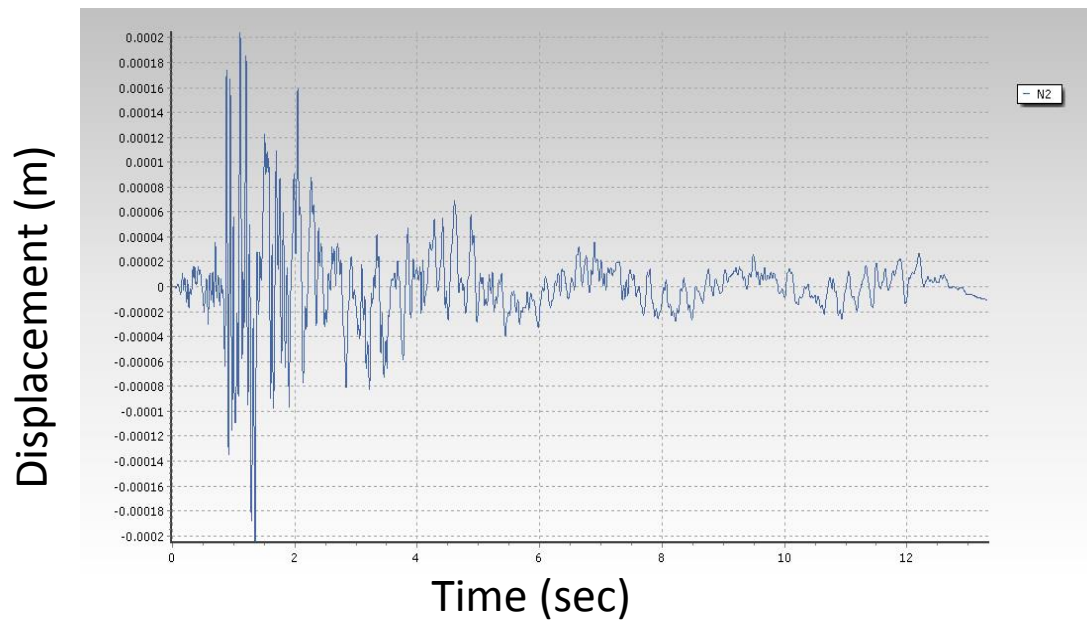
**Graph 5.6: Velocity Curve (Fault Normal)**



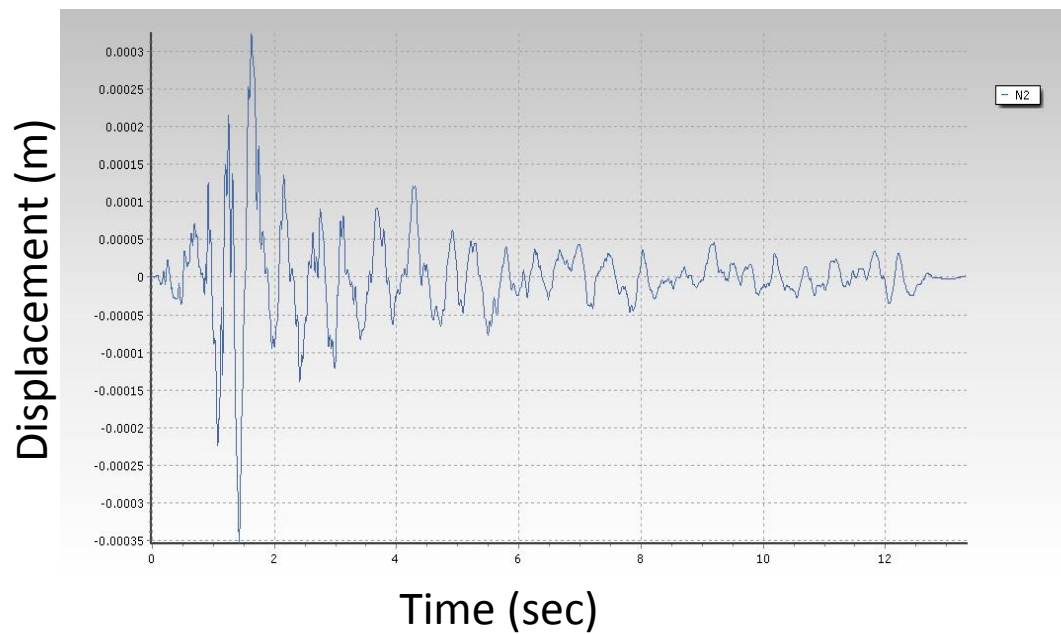
**Graph 5.7: Velocity curve (Fault parallel)**



**Graph 5.8: Displacement Curve (Fault Normal & Fault Parallel)**



**Graph 5.9: Displacement Curve (Fault Normal)**



**Graph 5.10: Displacement Curve (Fault Parallel)**

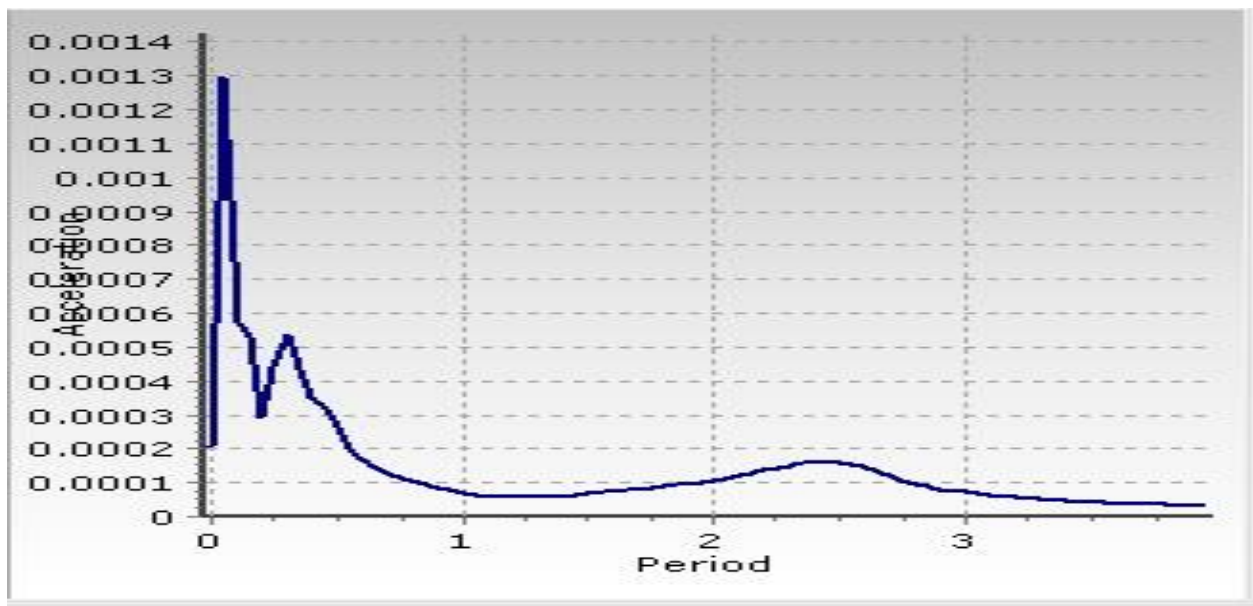
Finally the values of PGA, PGV and PGD for Fault Normal Ground motion and Fault Parallel components of far fault Ground motions are tabulated below:

Parameters	Fault Normal Ground motion	Fault Parallel Ground motion
PGA	0.1825 g	0.14 g
PGV	0.0172 m/s	0.0111 m/s
PGD	0.000204 m	0.000323 m

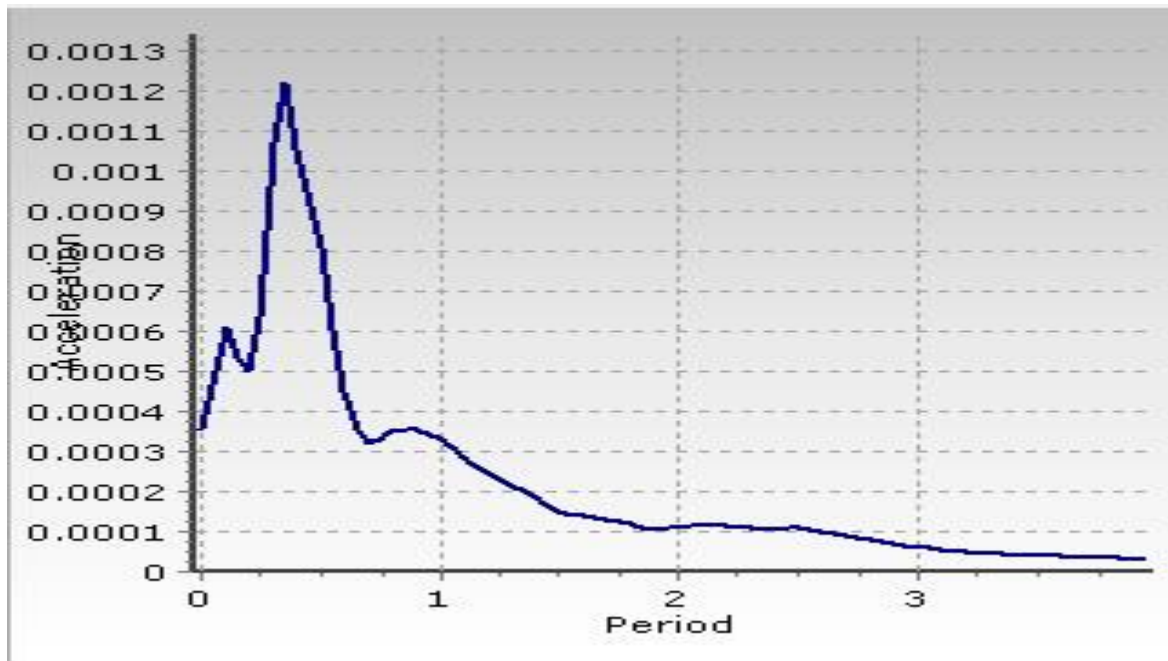
#### 5.2.2.2 Response spectrum Analysis:

Now, the effect of the downloaded input ground motion data has been investigated on the structure (SDF system) using the response spectrum analysis.

After performing response spectrum analysis we have got the output data for both fault normal and fault parallel components of Far Fault ground motions, and also the response spectrum curves were obtained which are shown in the following figures:



**Graph 5.11: Response spectrum curve (Fault normal)**

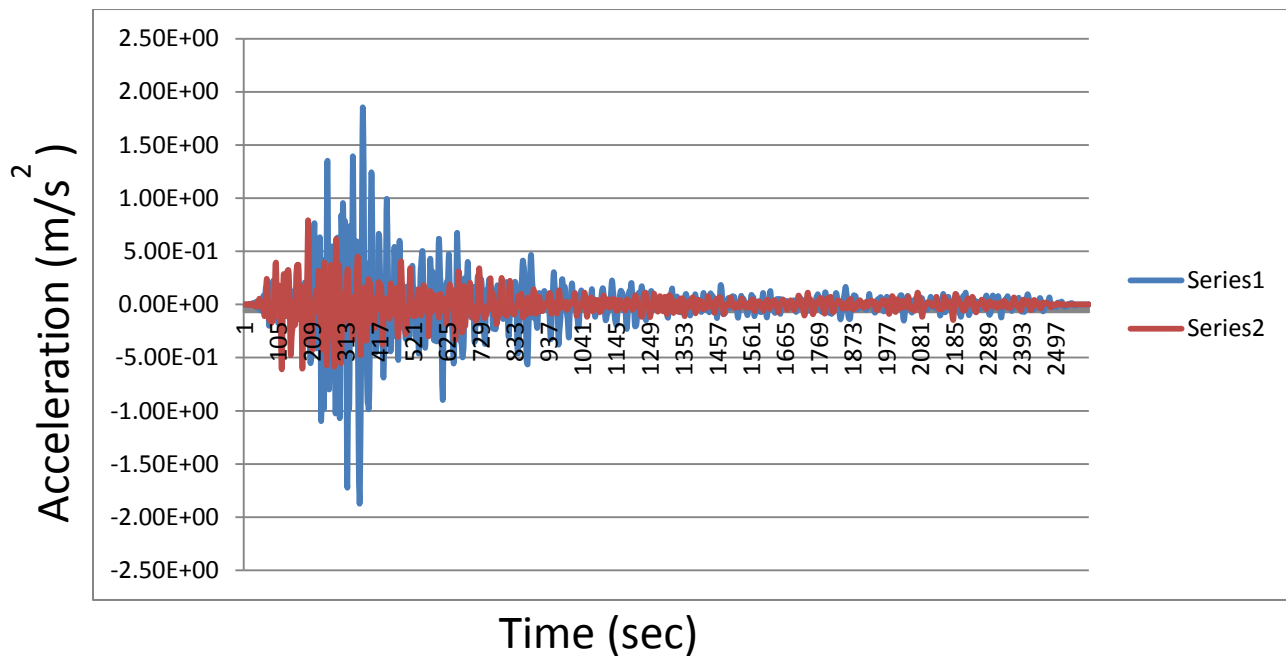


**Graph 5.12: Response spectrum curve (Fault parallel)**

## 5.3 Near Fault Earthquake:

### 5.3.1 Input data:

The analysis are performed for 2 sets of ground motion records (FN and FP) for the OROVILLE 08/08/75 07:00, JOHNSON RANCH, (CDMG STATION 1493). The acceleration time history was recorded for every 0.005 seconds.



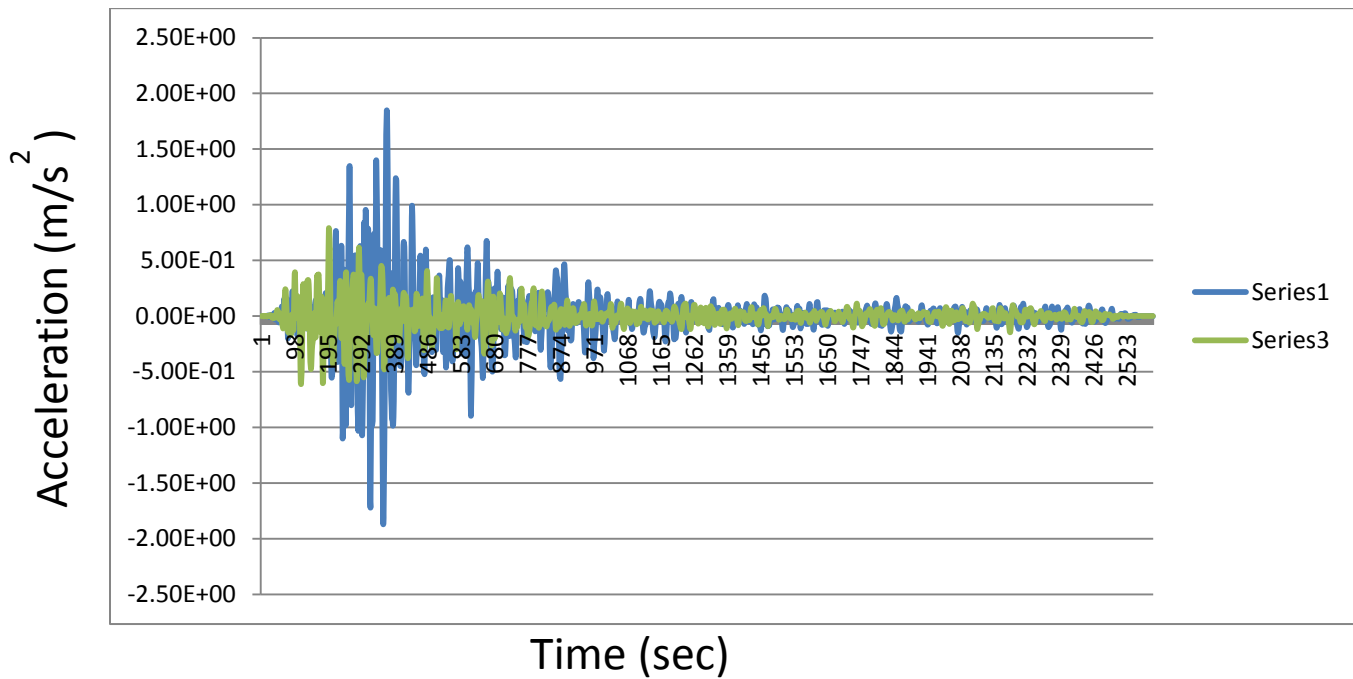
**Graph 5.13: Acceleration curve (Fault Normal & fault parallel Input data)**

### 5.3.2 Output data:

#### 5.3.2.1 Time History Analysis:

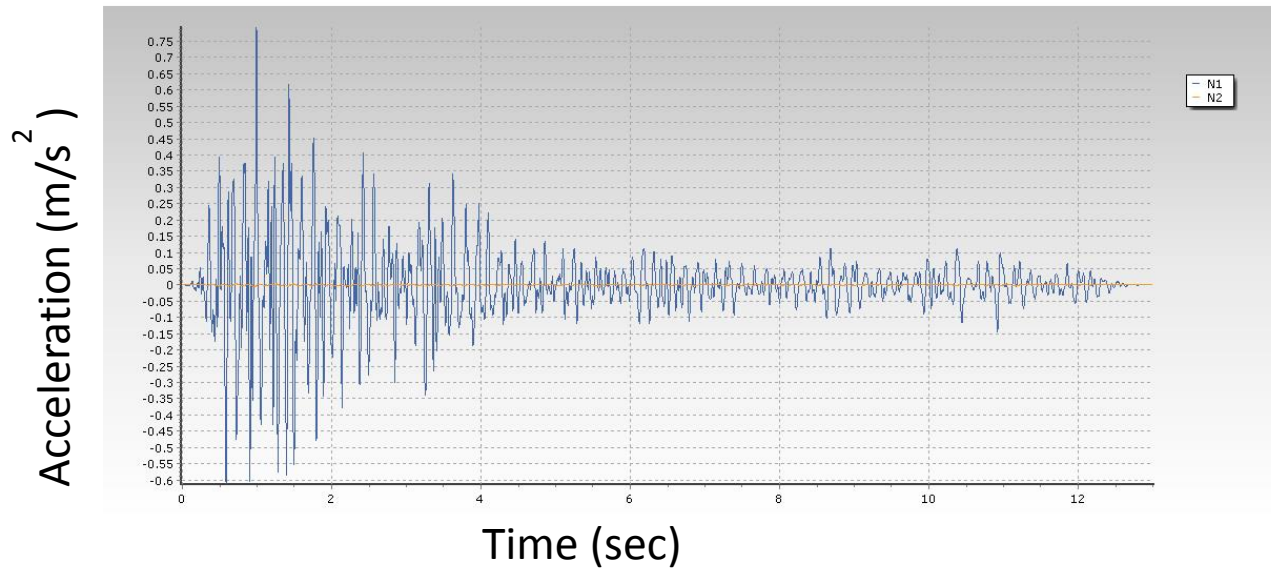
The effect of the downloaded input ground motion data has been investigated on the structure (SDF system) using the dynamic time history analysis.

After performing the dynamic time history analysis we have got the output data for both fault normal and fault parallel components of Near Fault ground motions , and also the curves for (acceleration, velocity and displacement) versus time were obtained which are shown in the following figures:

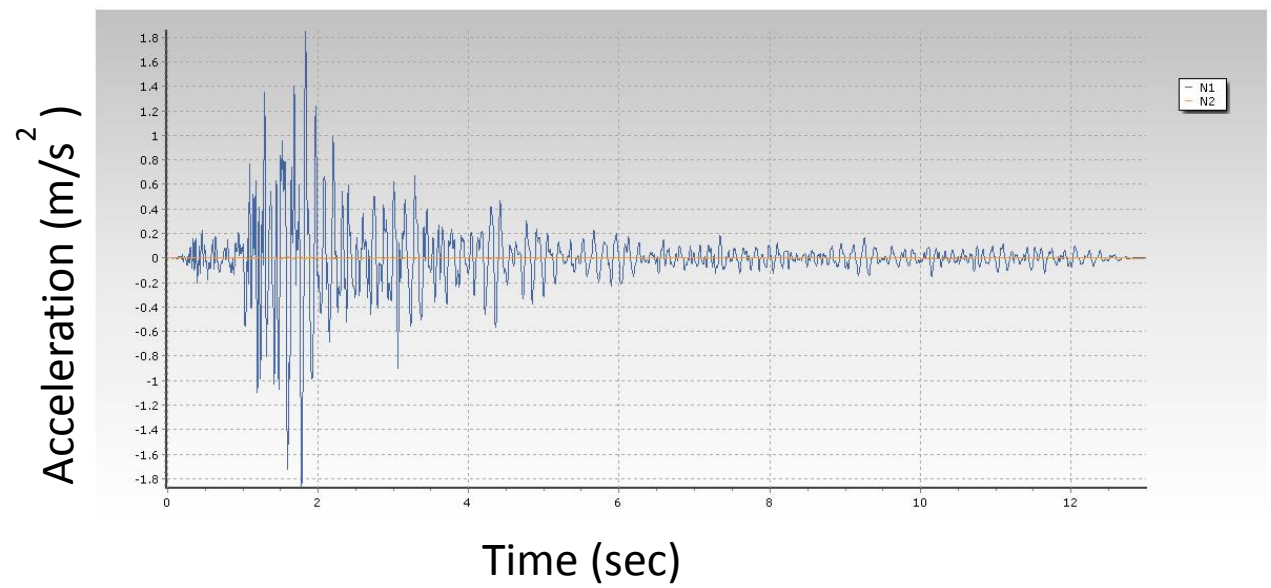


**Graph 5.14: Acceleration curve (Fault Normal & fault parallel)**

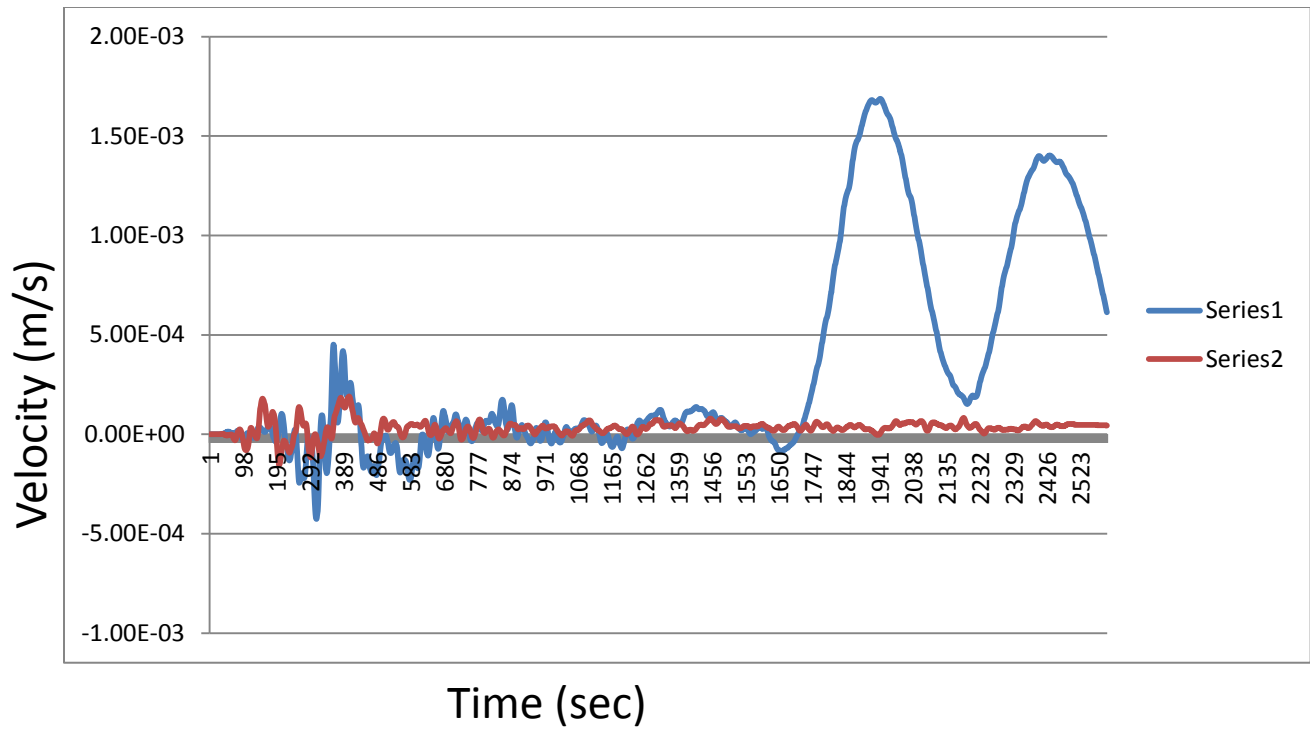




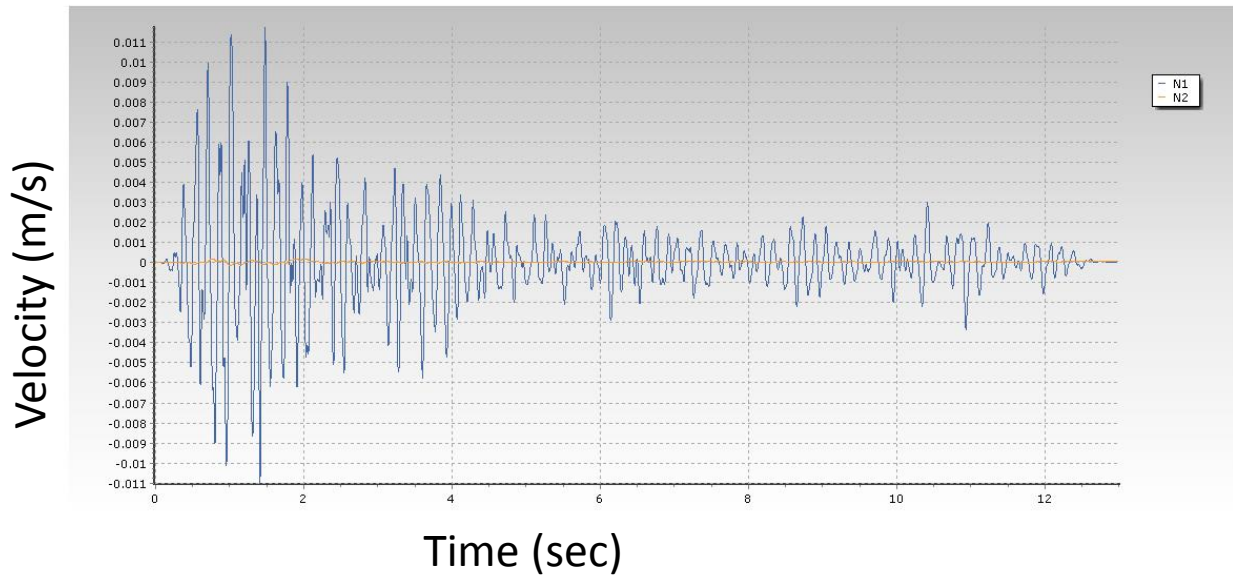
**Graph 5.15: Acceleration curve (Fault Normal)**



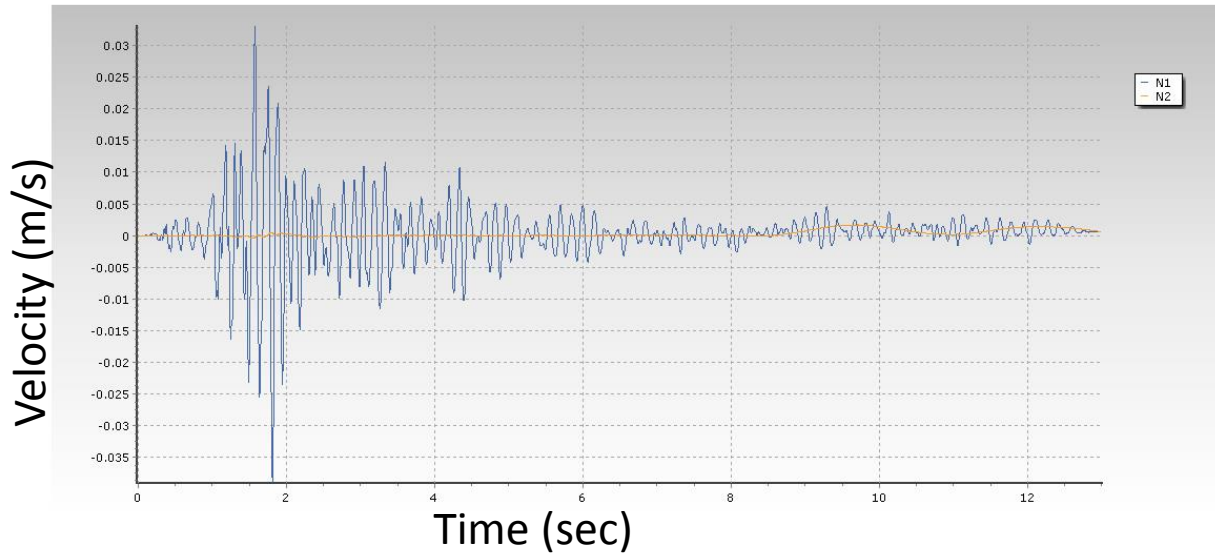
**Graph 5.16: Acceleration curve (Fault Parallel)**



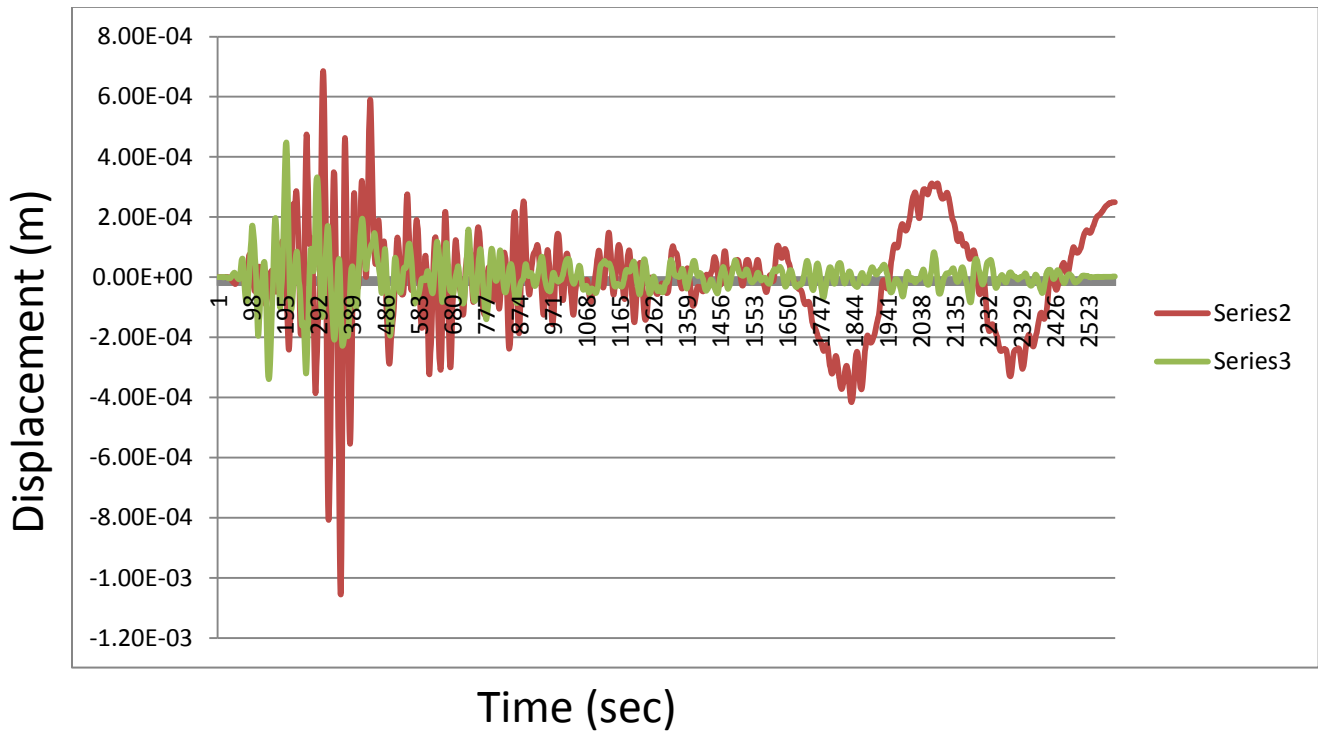
**Graph 5.17: Velocity Curve (Fault Normal & Fault Parallel)**



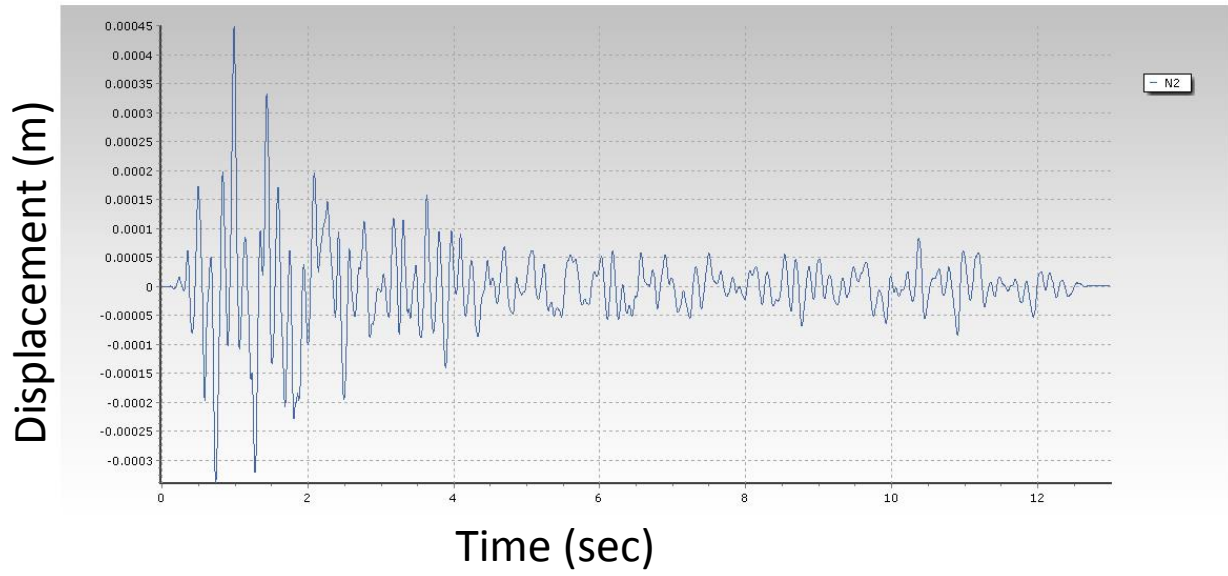
**Graph 5.18: Velocity Curve (Fault Normal)**



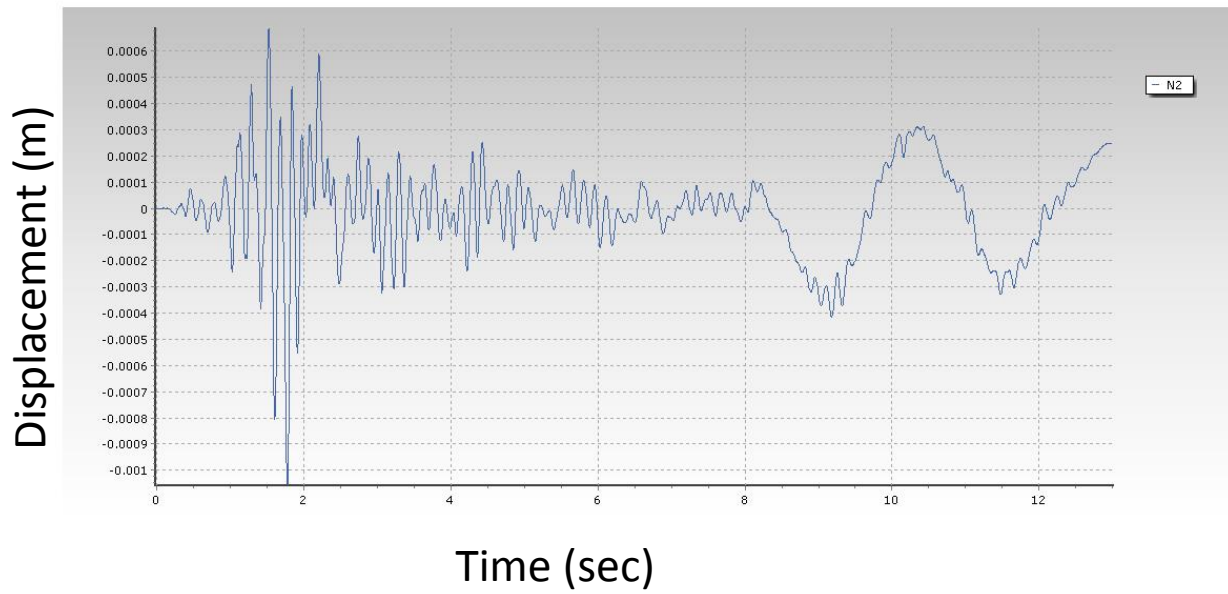
**Graph 5.19: Velocity curve (Fault parallel)**



**Graph 5.20: Displacement Curve (Fault Normal & Fault Parallel)**



**Graph 5.21: Displacement Curve (Fault Normal)**



**Graph 5.22: Displacement Curve (Fault Parallel)**

Finally the values of PGA, PGV and PGD for Fault Normal Ground motion and Fault Parallel components of near fault Ground motions are tabulated below:

Parameters	Fault Normal Ground motion	Fault Parallel Ground motion
PGA	0.1885 g	0.0805 g
PGV	0.00169m/s	0.00019 m/s
PGD	0.00069 m	0.00045 m

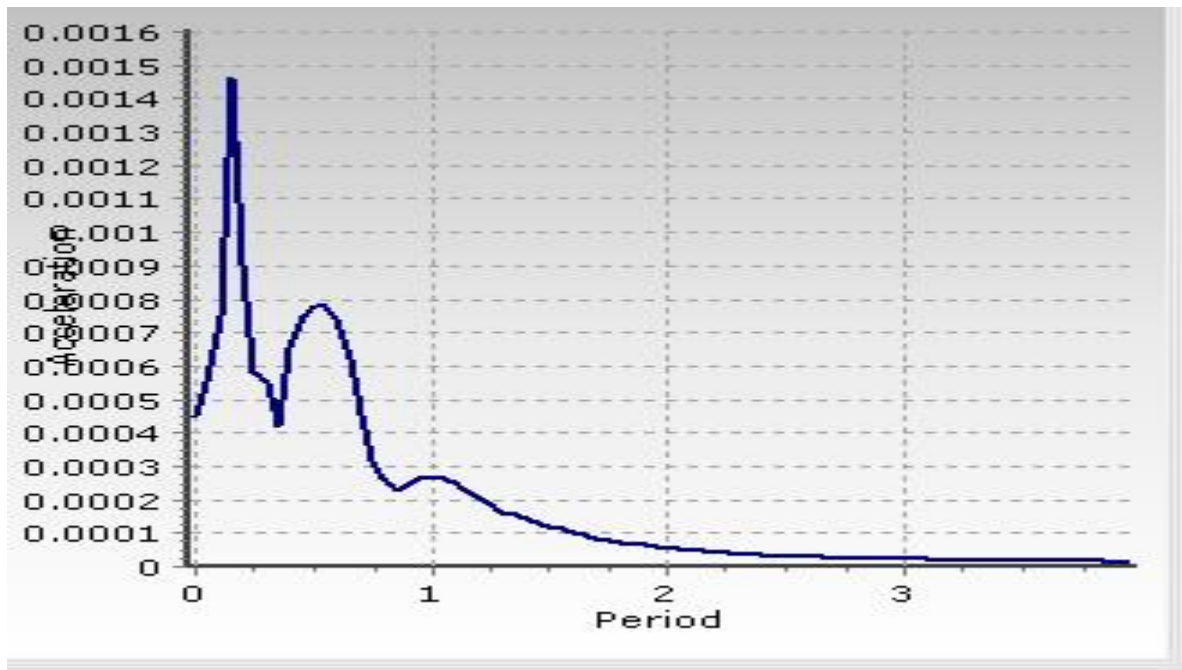
### 5.3.2.2 Response spectrum Analysis:

Now, the effect of the downloaded input ground motion data has been investigated on the structure (SDF system) using the response spectrum analysis.

After performing response spectrum analysis we have got the output data for both fault normal and fault parallel components of Near Fault ground motions, and also the response spectrum curves were obtained which are shown in the following figures:



**Graph 5.23: Response spectrum curve (Fault normal)**



**Graph 5.24: Response spectrum curve (Fault Parallel)**

# **CHAPTER 6**

## **SUMMARY AND CONCLUSION**

## **6.1 SUMMARY:**

In the current study the performance of a structure in a single degree of freedom system is investigated under different ground motions such as Fault normal and Fault parallel component of the ground motion by dynamic time history analysis method and the analysis is done in the SEISMOSTRUCT software developed by the SEISMOSOFT Company.

The Acceleration, Velocity and displacement curves have been drawn for both Fault Normal and Fault Parallel component of Far Fault and Near Fault ground motion. The values of acceleration, velocity, displacement have been found in every 0.005 seconds, also the values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement has been determined for both components.

Finally the response spectrum curves have been drawn for each kind of earthquake ground motions.

## **6.2 CONCLUSION:**

- The values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement obtained for fault normal component are higher than that of fault parallel component.
- The frequencies for fault normal component are higher than that of the fault parallel.
- The values of Peak Ground Acceleration, Peak Ground Velocity and Peak Ground Displacement of Fault Normal and Fault parallel components don't differ much for Far Fault earthquake ground motions, but they differ much for Near Fault Earthquake ground motions.
- The response spectrum curves are different for each kind of earthquake ground motions, hence it means that the structure have different responses to each kind of earthquake ground motions.



# **CHAPTER 7**

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